Improving Control of Dexterous Hand Prostheses Using Adaptive Learning

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Abstract—At the time of writing, the main means of control for polyarticulated self-powered hand prostheses is surface electromyography (sEMG). In the clinical setting, data collected from two electrodes are used to guide the hand movements selecting among a finite number of postures. Ever since the 60s though, machine learning has been applied to the sEMG signal (not in the clinical setting) with interesting results which provide more insight on how these data could be used to improve the prostheses functionality. Researchers have mainly concentrated so far on increasing the accuracy of sEMG classification and/or regression, but in general, a finer control implies a longer training period. A desirable characteristic would be to shorten the time needed by a patient for learning how to use the prosthesis.

To this aim, we propose here a general method to re-use past experience, in the form of models synthesised from previous subjects, to boost the adaptivity of the prosthesis. Extensive tests on databases recorded from healthy subjects in controlled and non-controlled conditions reveal that the method significantly improves the results over the baseline, non-adaptive case. This promising approach could be employed to pre-train a prosthesis before shipping it to a patient, leading to shorter training phase.

Index Terms—learning and adaptive systems, prosthetics, electromyography, human-computer interfaces

I. INTRODUCTION

I N the prosthetics/rehabilitation robotics community it is generally understood nowadays [1], [2], [3] that advanced hand prostheses are in dire need of accurate and reliable control schemas to make them easy to use by the patient. Together with excessive weight and low reliability, *lack of control* is the main reason why 30% to 50% of upper-limb amputees do not use their prosthesis regularly [4], although the exact factors leading to abandonement of a prosthesis depends on the age and status of each subject, remaining to be thoroughly investigated [5].

The force-controlled and polyarticulated hand prosethesis currently being used in the clinical setting, although not yet comparable with non-prosthetic mechanical hands, enjoy a high level of dexterity meaning that they have five fingers and can potentially achieve an infinite number of configurations, e.g., the *BeBionic* hand by RSL Steeper (www.bebionic.com), Vincent Systems' *Vincent hand* (www.handprothese.de) and the *i-LIMB* by Touch Bionics (www.touchbionics.com, see



Fig. 1. Dexterous hand prostheses: (left to right) RSL Steeper's *BeBionic* (reproduced from www.bebionic.com), Vincent Systems' *Vincent hand* (www.handprothese.de) and Touch Bionics's *i-LIMB Ultra* (www.touchbionics.com).

Figure 1). Yet, control by the patient is poor, and it is still enforced using two surface electromyography (sEMG) electrodes and complex sequences of muscle contraction impulses; this is essentially an old control schema enforced since the 60s [6], [7], [8]. The patient must get acquainted and proficient with this "language" if (s)he wants to achieve a minimum control over the prosthesis.

To overcome this drawback, a more "natural" form of control has been individuated and studied since two decades; namely, sEMG has been revamped by the application of machine learning techniques. More electrodes (typically 5+) and complex statistical classification/regression techniques (e.g., support vector machines [9], linear discriminants [10], [11], neural networks [12]) enable to detect, at least in principle, what the patient wants to do and to enforce it. The word "natural" here is still quite a misnomer, as it refers to the choice among a finite number of predefined hand configurations; but this kind of control is still much more natural than before, as each posture is achieved by configuring one's muscle remnants as they would be if the missing limb were still there. Recent results on amputees indicate that even longterm patients can generate rather precise residual activity, to the extent that there is essentially no statistically significant difference in the classification/regression accuracy attained by trans-radial amputees and intact subjects [9], [13].

In this paper we concentrate upon a specific aspect of hand prostheses control, namely, we try to reduce the *training time*, i.e. the time required to perform the adaptation of the prosthesis itself to the patient. Anatomical similarity among humans intuitively suggests that good statistical models built in the past might be proficiently reused when training a prosthesis for a new patient. This idea cannot be naïvely enforced with standard learning techniques, as shown at least in [14], where cross-subject analysis (i.e., using a model trained on

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a subject to do prediction on a new subject) is performed with poor results. We present here a more refined approach to the problem exploiting *adaptive learning* in order to boost the training phase of a hand prosthesis by reusing previous experience.

We build on our own previous work [15] which proposed a principled method to choose one among multiple pre-trained models on a known subjects as source for adaptation, and to evaluate the right degree of closeness to the target task for a new subject. This approach was based on an estimate of the model generalization ability through the leave-one-out error which was minimized solving a non convex optimization task. Here we improve the original method into two key aspects: (1) we constrain the new model, to be close to a linear combination of pre-trained models stored in the memory of the prosthesis; (2) the learning process to define from whom and how much to adapt is now defined through a convex optimization problem avoiding local minima issues. This translates into a consistent bootstrapping of the control abilities of the new subject, which can therefore acquire control of the device within a time range of at least one order of magnitude lower than what would be achieved without adaptation.

We test our method on two databases. The first is the one already described in [14], [15], consisting of sEMG, posture and force signals gathered from 10 intact subjects in various (controlled, non-controlled) laboratory situations. The second is the NinaPro database [16], a publicly available database which contains kinematic and sEMG data from the upper limbs of 27 intact subjects while performing a total of 52 hand postures. The benefits are apparent and the perspective is that of shipping a pre-trained prosthesis which would very quickly adapt to the patient, with the effect of enabling him/her to a higher comfort and aid during daily-life activities.

The paper is organised as follows: after reviewing related work, in Sections II and III we present the method. Section IV describes the database used, while Section V shows and discusses the results. Lastly, Section VI contains conclusions and ideas for the future work.

A. Related work

1) Using sEMG for hand prostheses: Surface EMG detects muscle unit activation potentials, which tipically present a quasi linear relation with the force exerted by the muscle to which the electrode is applied. In the more specific case of hand prostheses, several electrodes are applied to the forearm (or stump) while the subject reaches specific hand configurations (postures) and/or grabs a force sensor. The raw sEMG signal is then preprocessed (filtered, rectified, subsampled); features are subsequently extracted from it and fed, together with force values and labels denoting the postures, to a (usually supervised) machine learning method. Hand postures can be classified accordingly, and the force applied is predicted using a regression scheme. The two things can happen simultaneously [17]. Up to 12 hand postures [13] have been classified with acceptable accuracy, and there are strong hints [18], [9], [13], [19], [20] that with data from trans-radial amputees it may be possible to achieve similar performance.

Almost comprehensive surveys can be found in [21], [2], [3] and the most recent results at the time of writing are probably those exposed in [22], [23], [24] and [25]. The use of sEMG has been widely explored and a number of possible features have been extracted and tested with many machine learning methods.

2) Adaptive learning: One of the main assumption of machine learning is that the training data on which any method is learned and the test data on which it is verified are drawn from the same distribution. However, in real problems this is not always the case and adaptive learning is used to overcome the distribution mismatch. In particular transfer learning [26] and domain adaptation [27] face two aspects of this problem. The first focus mostly on binary tasks and on the use of helpful information across different categories (class with different labels). The second consider the possiblity to exploit common information among slightly different tasks when the set of label is the same. By applying domain adaptation, data collected in different domains can be used together (source + target) or it is possible to leverage on pre-trained models built on rich training sets (source) when facing the same problem in a new domain with few available samples (target).

In the last years, various techniques for transfer learning and domain adaptation have gathered attention in natural language processing [28], [29], computer vision [30], [31] and sentiment classification [32], [33]. Many adaptive methods have been compared and benchmarked in [29], however most of them are computationally inefficient because it is necessary to retrain each time over old source and new target data. An approach that does not use re-training, based on SVM has been proposed in [34]. However this technique does not take properly into account the possibility that the known model can be too different with respect to the new one due to high variability among the domains.

3) Adaptive learning on sEMG data: As already stated, any general-purpose method to augment the prostheses control and in particular to speed up the training time/aid the collection of training data is highly desirable. This problem can be casted in the adaptive learning framework.

One interesting attempt in this direction can be found in [35], where two adapting methods (one supervised, one unsupervised) are shown to dramatically outperform a nonadaptive approach.

The solution of adapting from data collected on different subjects is adopted in [36]: decoupling between subjectdependent and a motion-dependent components is enforced on a limited dataset, and an improvement over the baseline method is shown. In [37] samples from multiple source subjects are combined to the target subject samples. When learning the final classifier on the whole set of data a weighting factor is added to evaluate the real relevance of each source with respect to the target task. The sensibility of the method to this parameter is evaluated empirically, but how to choose it is left as an open problem.

In [15] we proposed an approach that exploited previously trained models on known subjects as starting point when learning on a new one. This method chooses automatically the best prior knowledge to use and how much to rely on it, overcoming at the same time the problems present in [37] and [34]. Compared with [35] that performs adaptation *during* the prediction task, our algorithm defines a way of boosting the performance in training, i.e. *before* beginning the prediction. We propose here to enlarge the approach in [15], even building over our [31] that shares the same basic mathematical framework. Specifically we propose a novel multiclass adaptive learning method able to rely over many prior knowledge models at the same time, with the aim to exploit at the best all the available information.

II. DEFINING THE ADAPTIVE MODEL

In this section we describe the mathematical framework at the basis of our adaptive learning method. We first introduce the basic notation (Section II-A), then we present our algorithm for online model adaptation from the best known subject (Section II-B) and how to enlarge it to exploit multiple known subjects (Sections II-C). We end explaining how to extend the described approach in the multiclass setting (Section II-D).

In the following we denote with small and capital bold letters respectively column vectors and matrices, e.g. $\boldsymbol{a} = [a_1, a_2, \ldots, a_N]^T \in \mathbb{R}^N$ and $\boldsymbol{A} \in \mathbb{R}^{G \times N}$ with A_{ji} corresponding to the (j, i) element. Moreover, we use a subscript to indicate a specific column of a matrix: e.g. \boldsymbol{A}_i is the *i*-th column of the matrix \boldsymbol{A} .

A. Background

Assume $x_i \in \mathbb{R}^m$ is an input vector and $y_i \in \mathbb{R}$ is its associated output. Given a set $\{x_i, y_i\}_{i=1}^N$ of samples drawn from an unknown probability distribution, we want to find a function f(x) such that it determines the best corresponding y for any future sample x. This is a general framework that includes both regression and classification. The problem can be solved in various ways. Here we will use kernel methods and in particular Least-Squares Support Vector Machines (LS-SVM, [38]). In LS-SVM the function f(x) is built as a linear model $\mathbf{w} \cdot \phi(\mathbf{x}) + b$, where $\phi(\cdot)$ is a nonlinear function mapping input samples to a high-dimensional (possibly infinite-dimensional) Hilbert space called feature space. Rather than being directly specified, the feature space is usually induced by a kernel function K(x, x') which evaluates the inner product of two samples in the feature space itself, i.e. $K(\boldsymbol{x}, \boldsymbol{x}') = \phi(\boldsymbol{x}) \cdot \phi(\boldsymbol{x}')$. A common kernel function is the Gaussian kernel:

$$K(\boldsymbol{x}, \boldsymbol{x}') = \exp(-\gamma ||\boldsymbol{x} - \boldsymbol{x}'||^2)$$
(1)

that will be used in all our experiments.

The parameters of the linear model, \mathbf{w} and b, are found by minimizing a regularized least-squares loss function [38]. This approach is similar to the well-known formulation of Support Vector Machines (SVMs), the difference being that the loss function is the square loss. Note that, contrary to SVMs, LS-SVMs do not induce sparse solutions.

This formulation can be easily generalized to the multiclass classification, where we have $g = 1, \ldots, G$ different classes. Consider one model for each class, w_g and b_g , that discriminates one class against the others (one-vs-all). Hence model g is trained on the binary problem to distinguish class g considered as positive, from all the others, considered negative. The predicted class for sample i is then defined as $\arg\max_{g} \{\mathbf{w}_{g} \cdot \phi(\mathbf{x}_{i}) + b_{g}\}.$

A key concept that we will use is the one of leaveone-out predictions [39]. Denote by \tilde{y}_i , i = 1, ..., N, the prediction on sample *i* when it is removed from the training set and by $\ell(y, \tilde{y})$ a generic loss function that measures the loss of predicting \tilde{y} when the true label is *y*. We have that $\frac{1}{N} \sum_{i=1}^{N} \ell(y_i, \tilde{y}_i)$ is an almost unbiased estimator of the classifier generalization error [40], measured using ℓ .

LS-SVMs make it possible to write the leave-one-out predictions in closed form and with a negligible additional computational cost [39]. This property is useful to find the best parameters for learning (e.g. γ in (1)) and it will be used in our adaptation method. Note that we use the same general formulation to solve both regression and classification problems.

B. Model Adaptation from the Best Subject

Let us assume we have K pre-trained models stored in memory, trained off-line on data acquired on K different subjects. When the prosthetic hand starts to be used by subject K + 1, the system begins to acquire new data. Given the differences among the subjects' arms and as well in the placement of the electrodes, these new data will belong to a new probability distribution, in general different from the Kpreviously modeled and stored. Still, as all subjects perform the same grasp types, it is reasonable to expect that the new distribution will be *close* to at least one of those already modeled; then, it should be possible to use one of the pretrained model as a *starting point* for training on the new data. We expect that, by doing so, learning should be faster than using the new data alone. To solve this problem we generalize the adaptation approach proposed in [34] for SVMs: the basic idea is to slightly change the regularization term of the SVM cost functional, so that the solution will be close to the pretrained one. The optimization problem is [34]:

$$\min_{\mathbf{w},b} \ \frac{1}{2} \|\mathbf{w} - \hat{\mathbf{w}}\|^2 + C \sum_{i=1}^N \xi_i$$

subject to $\xi_i \ge 0, \ y_i(\mathbf{w} \cdot \phi(\mathbf{x}_i) + b) \ge 1 - \xi_i$ (2)

where $\hat{\mathbf{w}}$ is a pre-trained model and *C* is a parameter to trade-off the errors and the regularization. In order to tune the closeness of \mathbf{w} to $\hat{\mathbf{w}}$, we introduce a scaling factor β weighing the pre-trained model; also, we use the square loss and therefore resort to the LS-SVM formulation. In this way the leave-one-out predictions can be evaluated in closed form, enabling automatic tuning of β . The optimization problem reads now like this [15]:

$$\min_{\mathbf{w},b} \frac{1}{2} \|\mathbf{w} - \beta \hat{\mathbf{w}}\|^2 + \frac{C}{2} \sum_{i=1}^{N} \xi_i^2$$

subject to $y_i = \mathbf{w} \cdot \phi(\mathbf{x}_i) + b + \xi_i$ (3)

and the corresponding Lagrangian problem is:

$$\mathcal{L} = \frac{1}{2} \|\mathbf{w} - \beta \hat{\mathbf{w}}\|^2 + \frac{C}{2} \sum_{i=1}^{N} \xi_i^2 - \sum_{i=1}^{N} a_i \{\mathbf{w} \cdot \phi(\mathbf{x}_i) + b + \xi_i - y_i\},$$
(4)

where $a \in \mathbb{R}^N$ is the vector of Lagrange multipliers. The optimality conditions can be expressed as:

$$\frac{\partial \mathcal{L}}{\partial \mathbf{w}} = \mathbf{0} \implies \mathbf{w} = \beta \hat{\mathbf{w}} + \sum_{i=1}^{N} a_i \phi(\mathbf{x}_i) , \qquad (5)$$

$$\frac{\partial \mathcal{L}}{\partial b} = 0 \implies \sum_{i=1}^{N} a_i = 0 , \qquad (6)$$

$$\frac{\partial \mathcal{L}}{\partial \xi_i} = 0 \implies a_i = C\xi_i , \qquad (7)$$

$$\frac{\partial \mathcal{L}}{\partial a_i} = 0 \implies \mathbf{w} \cdot \phi(\mathbf{x}_i) + b + \xi_i - y_i = 0.$$
 (8)

From (5) it is clear that the adapted model is given by the sum of the pre-trained model $\hat{\mathbf{w}}$ (weighted by β) and a new model \mathbf{w} obtained from the new samples. Note that when β is 0 we recover the original LS-SVM formulation without any adaptation to previous data. Using (5) and (7) to eliminate \mathbf{w} and $\boldsymbol{\xi}$ from (8) we find that:

$$\sum_{j=1}^{N} a_j \ \phi(\boldsymbol{x}_j) \cdot \phi(\boldsymbol{x}_i) + b + \frac{a_i}{C} = y_i - \beta \hat{\mathbf{w}} \cdot \phi(\boldsymbol{x}_i) \ . \tag{9}$$

Denoting with K the kernel matrix, i.e. $K_{ji} = K(x_j, x_i) = \phi(x_j) \cdot \phi(x_i)$, the obtained system of linear equations can be written more concisely in matrix form as:

$$\begin{bmatrix} \mathbf{K} + \frac{1}{C}\mathbf{I} & \mathbf{1} \\ \mathbf{1}^{T} & 0 \end{bmatrix} \begin{bmatrix} \mathbf{a} \\ b \end{bmatrix} = \begin{bmatrix} \mathbf{y} - \beta \hat{\mathbf{y}} \\ 0 \end{bmatrix}, \quad (10)$$

where \boldsymbol{y} and $\hat{\boldsymbol{y}}$ are the vectors containing respectively the label samples and the prediction of the previous model i.e. $\boldsymbol{y} = [\boldsymbol{y}_1, \dots, \boldsymbol{y}_N]^T$, $\hat{\boldsymbol{y}} = [\hat{\boldsymbol{w}} \cdot \boldsymbol{\phi}(\boldsymbol{x}_1), \dots, \hat{\boldsymbol{w}} \cdot \boldsymbol{\phi}(\boldsymbol{x}_N)]^T$. Thus the model parameters can be calculated with:

$$\begin{bmatrix} a \\ b \end{bmatrix} = \boldsymbol{P} \begin{bmatrix} \boldsymbol{y} - \beta \hat{\boldsymbol{y}} \\ 0 \end{bmatrix}, \qquad (11)$$

where $P = M^{-1}$ and M is the first matrix on the left in (10).

We now show that for (3) it is possible to write the leave-one-out predictions in a closed formula (proof in the Appendix). Let $[a'^T, b']^T = P[y^T, 0]^T$ and $[a''^T, b'']^T = P[\hat{y}^T, 0]^T$ with $a = a' + \beta a''$, then

Proposition 1. The prediction \tilde{y}_i , obtained on sample *i* when *it is removed from the training set, is equal to*

$$y_i - \frac{a'_i}{P_{ii}} + \beta \frac{a''_i}{P_{ii}}$$
 (12)

Notice that in the above formula β is the only parameter, hence, it is possible to set it optimally in order to minimize the sum of the leave-one-out errors $\ell(y_i, \tilde{y}_i)$, while at the same time choosing the best pre-trained model for adaptation. Moreover, *a* depends linearly on β , thus it is straightforward to define the learning model which is fixed once β has been chosen. The complexity of the algorithm is dominated by the evaluation of the matrix P, which must anyway occur while training; thus, the computational complexity of evaluating the leaveone-out errors is negligible, if compared to the complexity of training. As a last remark, we underline that the pre-trained model $\hat{\mathbf{w}}$ can be obtained by any training algorithm, as far as it can be expressed as a weighted sum of kernel functions. The framework is therefore very general.

C. Model Adaptation from Multiple Subjects

The approach described in the previous Section has a main drawback: although many prior knowledge models are available, it uses only one of them, selected as the most useful in term of minimal leave-one-out errors. Even if the pre-trained models are not equally informative, relying on more than one of them may be beneficial. To this goal it is possible to define a new learning problem which considers the linear combination of all the known models [31]:

$$\min_{\mathbf{w},b} \frac{1}{2} \left\| \mathbf{w} - \sum_{k=1}^{K} \beta^{k} \hat{\mathbf{w}}^{k} \right\|^{2} + \frac{C}{2} \sum_{i=1}^{N} \xi_{i}^{2}$$

subject to $y_{i} = \mathbf{w} \cdot \phi(\boldsymbol{x}_{i}) + b + \xi_{i}$. (13)

The original single coefficient β has been substituted with a vector β containing as many elements as the number of prior models, *K*. For this formulation the optimal solution is:

$$\mathbf{w} = \sum_{k=1}^{K} \beta^k \hat{\mathbf{w}}^k + \sum_{i=1}^{N} a_i \phi(\boldsymbol{x}_i) .$$
 (14)

Here w is expressed as a weighted sum of the pre-trained models scaled by the parameters β^k , plus the new model built on the incoming training data [31]. The leave-one-out prediction of each sample *i* can again be written in closed form, similarly to Proposition 1, as

$$\tilde{y}_i = y_i - \frac{a'_i}{P_{ii}} + \sum_{k=1}^K \beta^k \frac{a''^k}{P_{ii}},$$
(15)

where $[\mathbf{a}''^{kT}, b''^{k}]^{T} = \mathbf{P}[\hat{\mathbf{y}}^{kT}, 0]^{T}$ and $\hat{\mathbf{y}}^{k}$ is the vector which contains the predictions of the *k*-th previous model $[\hat{\mathbf{w}}^{k} \cdot \phi(\mathbf{x}_{1}), \dots, \hat{\mathbf{w}}^{k} \cdot \phi(\mathbf{x}_{N})]$. As before, the leave-one-out errors can be calculated and minimized to evaluate the best weights β^{k} .

D. Multiclass Extensions

In case of classification problems, the methods discussed till here are suitable for binary tasks but can be extended to the case of G classes using the one-vs-all formulation described in Section II-A. We define the matrix $\boldsymbol{Y} \in \mathbb{R}^{G \times N}$ composed by the columns \boldsymbol{Y}_i , where for each sample *i* the vector \boldsymbol{Y}_i has all the components equal to -1 except for the y_i -th that is equal to 1. In the same way, define the matrix $\hat{\boldsymbol{Y}}$, composed by the columns $\hat{\boldsymbol{Y}}_i$ that contain the predictions generated by a known multiclass model on the sample *i*. For each sample *i* we also obtain a vector of G leave-one-out predictions, we indicate it with $\tilde{\boldsymbol{Y}}_i$, and it is easy to show that it can be calculated as

$$\tilde{\boldsymbol{Y}}_{i} = \boldsymbol{Y}_{i} - \frac{\boldsymbol{A}_{i}'}{P_{ii}} + \beta \frac{\boldsymbol{A}_{i}''}{P_{ii}},$$
(16)

where

$$[\boldsymbol{A}',\boldsymbol{b}'] = [\boldsymbol{Y},\boldsymbol{0}]\boldsymbol{P}^T , \qquad (17)$$

$$[\mathbf{A}'', \mathbf{b}''] = [\hat{\mathbf{Y}}, \mathbf{0}] \mathbf{P}^T$$
 (18)

Here $A', A'' \in \mathbb{R}^{G \times N}$ and $b, 0 \in \mathbb{R}^{G}$. In case of multiple prior models, we use the superscript k to indicate each of them and, considering their linear combination, we get

$$\tilde{\boldsymbol{Y}}_{i} = \boldsymbol{Y}_{i} - \frac{\boldsymbol{A}_{i}'}{P_{ii}} + \sum_{k=1}^{K} \beta^{k} \frac{\boldsymbol{A}_{i}''^{k}}{P_{ii}}, \qquad (19)$$

with

$$[\boldsymbol{A}^{\prime\prime k}, \boldsymbol{b}^{\prime\prime k}] = [\hat{\boldsymbol{Y}}^{k}, \boldsymbol{0}] \boldsymbol{P}^{T} . \qquad (20)$$

III. LEARNING HOW MUCH TO ADAPT

The adaptive learning methods described above look for the model parameters (\mathbf{w},b) once the value of the weight β , or the corresponding vector β , has been chosen. Searching the optimal β defines a separate learning problem which depends on the choice of the loss function ℓ . As a result we have an indication of how much each of the pre-trained models is reliable for adaptation. In the following we define how to face this issue in the classification and regression cases, a general scheme of the proposed solutions is in Figure 2.

A. Classification

For a binary classification problem, and in case of a single pre-trained model, we can follow the approach proposed in [39] and find β by minimizing leave-out-out errors using the logistic loss function:

$$\ell(y_i, \tilde{y}_i) = \frac{1}{1 + \exp(-10(\tilde{y}_i - y_i))} .$$
(21)

Note that the resulting objective function would be non-convex w.r.t. β . When moving to the choice of multiple weights for all the pre-trained models we can also overcome the non-convexity issue described above, by minimizing the loss function proposed in [31]:

$$\ell(y_i, \tilde{y}_i) = \max(1 - y_i \tilde{y}_i, 0), \tag{22}$$

this is a convex upper-bound to the misclassification loss and it also has a smoothing effect, similar to the logistic function in (21).

However in our application we have multiple pre-trained models and G classes, corresponding to the different grasp types. Hence it is necessary to define a loss function over vectors, that compose all these values to define a single estimate of the multiclass error.

1) Best Prior Model: A first solution could be to consider:

$$\ell(\boldsymbol{Y}_{i}, \tilde{\boldsymbol{Y}}_{i}) = \frac{1}{1 + \exp(-10(\max_{g \neq y_{i}}\{\tilde{Y}_{gi}\} - \tilde{Y}_{y_{i}i}))}, \quad (23)$$

and to evaluate it separately for each of the $k \in \{1, ..., K\}$ pre-trained models on the basis of (16), varying β with small steps in [0, 1] (this is the approach used in [15]). The minimal result identifies both the best known subject for adaptation and, at the same time, the corresponding β . Still, this approach, as (21), is non-convex thus reaching the global optimum is not computationally efficient. This solution is schematically depicted in Figure 2 (left).

2) *Multiple Prior Models:* To consider multiple prior knowledge models we propose to use (19) in the convex multiclass loss [41]:

$$\ell(\boldsymbol{Y}_i, \tilde{\boldsymbol{Y}}_i) = \max\{1 - \tilde{Y}_{y_i i} + \max_{g \neq y_i} \{\tilde{Y}_{gi}\}, 0\}, \quad (24)$$

with the final objective function:

$$\min_{\boldsymbol{\beta}} \sum_{i=1}^{N} \ell(\boldsymbol{Y}_i, \tilde{\boldsymbol{Y}}_i) \quad \text{subject to} \quad \|\boldsymbol{\beta}\|_2 \leq 1, \quad \beta_k \geq 0 \ . \ (25)$$

The condition of having β in the intersection of the unitary ball and the positive semi-plane can be seen as a form of regularization and it is a natural generalization of the original constraint $\beta \in [0, 1]$ used in [15]. This constraint is necessary to avoid overfitting problems which can happen when the number of known models is large compared to the number of training samples [31].

We implemented the optimization process using a simple projected sub-gradient descendent algorithm, where at each iteration β is first projected onto the l_2 -sphere, $\|\beta\|_2 \leq 1$ and then onto the positive semi-plane. The pseudo-code is in Algorithm 1, where in line 8 $1\{\cdot\}$ denotes the indicator function. Figure 2 (center) describes this solution.

3) Different Weights for Different Classes: Until now we considered techniques which assign a unique weight to each known subject. This means that, the whole set of one-vs-all pre-trained models for a subject are equally weighted. However, for example, when learning the model for the first class, it may be useful to give more weight in adaptation to the first subject than to the second, while it could be the opposite when learning the model for the second class, and so on. Hence, to have one more degree of freedom and decide the adaptation specifically for each class, we enlarge the set of weight parameters introducing the matrix $\mathbf{B} \in \mathbb{R}^{K \times G}$ where each row $k \in \{1, \ldots, K\}$ contains the vector $\boldsymbol{\beta}_k^T$ with G elements, one for each class. This approach is described in Figure 2 (right).

The optimization problem is analogous to the one described in (25), with a change in the constraints. Each class problem is now considered separately, so we have G conditions, one for each of the columns \mathbf{B}_g of the **B** matrix, we impose $\|\mathbf{B}_g\|_2 \le$ 1 and $B_{ji} \ge 0$.



Fig. 2. This figure shows the three methods adopted to leverage information from multiple known subjects when learning on a new one. For all the known subjects many sEMG signal samples are available, while few sEMG signals are recorded from the new subject. Left: choose only the best known subject and use its reweighted model as a starting point for learning. Center: consider a linear combination of the known subjects with equal weight for all the grasp models of each subject. Right: consider again a linear combination of all the known models but assign a different weight to each grasp model for each subject.

orithm

Algorithm 1Projected Sub-gradient Descent Algorith1:
$$\beta = [\beta_1 \dots \beta_K] \leftarrow 0$$
2: $t \leftarrow 1$ 3: calculate A' according to (17)4: calculate A''^k according to (20)5: repeat6: $\tilde{Y}_i \leftarrow Y_i - \frac{A'_i}{P_{ii}} + \sum_{k=1}^K \beta^k \frac{A''^k}{P_{ii}} \quad \forall i = 1, \dots, N$ 7: $g_i^* \leftarrow \operatorname{argmax}_{g \neq y_i} \{\tilde{Y}_{gi}\}, \quad \forall i = 1, \dots, N$ 8: $d_i \leftarrow \mathbf{1}\{1 - \tilde{Y}_{y_ii} + \tilde{Y}_{g_i^*i} > 0\}, \quad \forall i = 1, \dots, N$ 9: $\beta^k \leftarrow \beta^k - \frac{1}{\sqrt{t}} \sum_{i=1}^N d_i \frac{A''^k_{g_i^*i}}{P_{ii}}, \quad \forall k = 1, \dots, K$ 10: if $\|\beta\|_2 > 1$ then11: $\beta \leftarrow \beta/\|\beta\|_2$ 12: end if13: $\beta^k \leftarrow \max(\beta^k, 0), \quad \forall k = 1, \dots, K$

14:
$$l \leftarrow l + 1$$

15: until convergence

Output:
$$\beta$$

B. Regression

Our goal in using regression is the prediction of the force applied by one subject in grasping, independently to the specific kind of grasp performed. Thus now the output y_i for each corresponding input x_i is a continuous real value, rather a discrete one as in classification.

Similarly to what seen before, it is possible to learn the regression model relying on information from the closest known subject, or on the combination of multiple pre-trained

models.

1) Best Prior Model: We can use the leave-one-out prediction in (12) to evaluate the square loss (Mean Square Error MSE):

$$\ell(y_i, \tilde{y}_i) = (y_i - \tilde{y}_i)^2 = \left(\frac{a'_i}{P_{ii}} + \beta \frac{a''_i}{P_{ii}}\right)^2$$

The choice of the square loss gives us, summing over i, a quadratic function in β and the minimum is obtained using:

$$\beta = \frac{\sum_{i=1}^{N} \frac{a'_i}{P_{ii}} \frac{a''_i}{P_{ii}}}{\sum_{i=1}^{N} \left(\frac{a''_i}{P_{ii}}\right)^2} \,. \tag{26}$$

We use the constraint $\beta > 0$, just imposing $\beta = 0$ every time it results negative. Hence, differently from the classification case, here we do not need any optimization procedure, the optimal β is given by a closed formula. Once calculated the minimum value of the summed square loss values for each $k \in \{1, 2, \dots, K\}$, comparing all of them, we can identify the best known subject to use for adaptation when learning the regression model on a new subject.

2) Multiple Prior Models: To take advantage from all the available pre-trained models we can combine them linearly and search for a vector of weights as in classification. Hence the loss function ℓ can now be defined as

$$\ell(y_i, \tilde{y}_i) = \left(\frac{a'_i}{P_{ii}} + \sum_{k=1}^K \beta^k \frac{a''_i}{P_{ii}}\right)^2 .$$
 (27)

Adding also the condition $\|\beta\|_2 \leq 1$, we can find the best β vector which minimizes the loss with a Quadratically Constrained Quadratic Program (QCQP) solver. In our experiments we used CVX [42], a package for specifying and solving convex programs in MATLAB.



Fig. 3. The three different grasp type recorded in the hand posture and force signal dataset [14]: (a) index precision grip; (b) other fingers precision grip; (c) power grasp. Reproduced from [14].



Fig. 4. The six different grasp types extracted from the Ninapro dataset [16]: (a) tip pinch grasp; (b) prismatic four fingers grasp; (c) power grasp; (d) parallel extension grasp; (e) lateral grasp; (f) open a bottle with a tripod grasp. Reproduced from [16].

IV. EXPERIMENTAL DATA

To test the effectiveness of our model adaption techniques we use two datasets.

a) Hand posture and force signals [14]: This database of sEMG / hand posture / force signals has been already presented in [14], and used in [14], [15]. (The following description of the database is very concise; the interested reader should refer to the above cited paper(s) for more details.) The signals are collected from 10 intact subjects (2 women, 8 men) using 7 sEMG electrodes (Aurion ZeroWire wireless) placed on the dominant forearm according to the medical literature [43]. A FUTEK LMD500 force sensor [44] is used to measure the force applied by the subject's hand during the recording. Data are originally sampled at 2kHz. Each subject starts from a rest condition (sEMG baseline activity) then repeatedly grasps the force sensor using, in turn, three different grips, visible in Figure 3. The subject either remains seated and relaxed while performing the grasps, or is free to move (walk around, sit down stand up, etc.). These phases are referred to as Still-Arm (SA) and Free-Arm (FA) respectively. Each grasping action is repeated along 100 seconds of activity. The whole procedure is repeated twice. The root mean square of the signals along 1s (for classification) and 0.2s (for regression) is evaluated; subsampling at 25Hz follows. Samples for which the applied force is lower than 20% of the mean force value obtained for each subject are labeled as "rest" class. After this preprocessing we got around 15000 samples per subject, each sample consists of a 7 elements sEMG signal vector and one force value.

b) Ninapro [16]: This database has been presented in [16] and already used in [45]. It contains kinematic and sEMG

data from the upper limbs of 27 intact subjects (7 women, 20 men) while performing 12 finger, 9 wrist, 23 grasping and functional movements, plus 8 isometric, isotonic hand configurations. Data are collected using 10 surface sEMG electrodes (double-differential OttoBock MyoBock 13E200), 8 placed just beneath the elbow at fixed distance from the radio-humeral joint, while 2 are on the flextor and extensor muscles. Each subject sits confortably on an adjustable chair in front of a table and is instructed to perform ten repetitions of each movement by imitating a video, alternated with a rest phase. The sEMG electrodes are connected to a standard DAQ card sampling the signals at 100 Hz and provide an RMS rectified version of the raw sEMG signal. (For a more detailed description of the dataset the interested reader should refer to [16], [45]). We focused only on the grasp and functional movements extracting 6 actions: tip pinch, prismatic four fingers, power, parallel extension, lateral and open a bottle with a tripod grasp (see Figure 4). Each of them belongs to a different branch of a hierarchy containing all the dataset hand postures and the first three grasps are the most similar to the ones considered in [14]. We randomly extracted two sets of 10 and 20 subjects from the dataset and performed classification experiments on the described 7 class (6 grasps plus rest) problem considering the Mean Absolute Value (MAV) of the sEMG signal as time domain features [45]. We repeated the preprocessing and data split procedure described in [45] with an extra subsampling of the "rest" data to get a class-balanced setting.

V. EXPERIMENTAL RESULTS

As already mentioned in Section II-B, our working assumption is to have K pre-trained models stored in memory; new data comes from subject K + 1 and the system starts training, to build the K+1'th model. The performance is then evaluated using unseen data from subject K+1. To simulate this scenario and to have a reliable estimation of the performance, we use a leave-one-out approach: out of the 10(20) subjects for which we have data recordings, we train 9(19) models off-line. These correspond to the K stored models in memory, while data from the remaining subject are used for the adaptive learning of the K+1'th model. This procedure is repeated 10(20) times, using in turn all the recorded subjects for the adaptive learning of the model.

We name the proposed adaption methods respectively:

- *Best-Adapt*: adaptive learning starting from the best prior knowledge model (method originally presented in [15] and revised here in Section III-A1);
- *Multi-Adapt*: adaptive learning starting from a linear combination of the known models (Section III-A2);
- *Multi-perclass-Adapt*: adaptive learning (for classification) starting from a linear combination of the known models with a different weight for each class (Section III-A3).

To assess the performance of all these methods we compare them to three baseline approaches:

- *No-Adapt*: is plain LS-SVM using only the new data for training, as it would be in the standard scenario without adaption.
- *Prior Average*: consists in using only the pre-trained models without updating them with the new training data. We consider their average performance.
- *Prior Start*: this corresponds to the performance of the best model chosen by Best-Adapt at the first training step.
- *Prior Test*: this is the result that can be obtained *a posteriori* comparing all the prior knowledge models on the test set and choosing the best one.

As a measure of performance, for classification we use the standard classification rate; for regression, the performance index is the correlation coefficient evaluated between the predicted force signal and the real one. Although we minimized the MSE in the regression learning process, the choice of the correlation coefficient is suggested by a practical consideration: when driving a prosthesis, or even a non-prosthetic mechanical hand, we are not interested in the absolute force values desired by the subject: mechanical hands usually cannot apply as much force as human hands do, for obvious safety reasons, or e.g., in teleoperation scenarios, they could be able to apply much more force than a human hand can. As already done, e.g. in [17], [9], [14], we are rather concerned with getting a signal which is strongly correlated with the subject's will. The significance of the comparisons between the methods is evaluated through the sign test [46].

To build the pre-trained models we used the standard SVM algorithm. All the parameters to be set during training (C and γ of the Gaussian kernel) were chosen by cross-validation. Specifically when the subject k^* is the new problem, this is

excluded form the dataset and the parameters are chosen over the remaining set $\mathcal{K} = \{1, \ldots, K \setminus k^*\}$ looking for the values that produce on average the best recognition rate or correlation coefficient by learning on each subject k in \mathcal{K} and testing on $\{\mathcal{K} \setminus k^*, k\}$.

A. Hand posture and force signals [14]

For the experiments running on the dataset described in [14], the training sequences are random subsets from the entire dataset of the new subject, i.e. they are taken without considering the order in which they were acquired. We considered 24 successive learning steps, for each of them the number of available training samples increases by 30 elements reaching a maximum of 720 samples. The test runs over all the remaining samples. We conducted three sets of experiments considering different prior knowledge-new problem couples: SA-SA, FA-FA and SA-FA. In the first two cases we have consistent recording conditions among the source and the new target problem. The last case reproduces the more realistic scenario where the prior knowledge is built on data recorded on subjects in laboratory controlled conditions while the new subject moves freely. We both classify the grasp type and predict the force measured by the force sensor.

Figure 5 (left) reports the obtained classification rate at each step when using SA-SA data. The plot shows that Multiperclass-Adapt outperforms both the baselines No-Adapt, Priors, and all the other adaptive learning methods. The difference between Multi-perclass-Adapt and Best-Adapt shows an average advantage in recognition rate of around 2% (p < 0.03). The gain obtained by Multi-perclass-Adapt with respect to No-Adapt (p < 0.003) stabilizes around 5% for 500-720 training samples.

Analogous results are obtained when considering FA-FA data: Figure 5 (center) reports the classification rate results in this setting. Multi-perclass-Adapt shows again the best performance, but now the advantage with respect to Best-Adapt is significant (p < 0.03) only for less than 100 training samples. Multi-perclass-Adapt outperforms No-Adapt (p < 0.03) with a gain of 4% in recognition rate for 500-720 samples.

Finally, Figure 5 (right) shows the SA-FA results. Here the statistical comparison among Multi-perclass-Adapt, Best-Adapt and No-Adapt is the same as in the FA-FA case.

Analyzing Figure 5 as a whole, we can state that all the proposed adaptive methods outperform learning from scratch with the best results obtained when exploiting a linear combination of pre-trained models with a different weight for each known subject and each class (Multi-perclass-Adapt). Moreover, we notice that learning with adaption with 30 training samples performs almost as No-Adapt with around 300 samples. Considering the acquisition time, this means that the adaptive methods are almost ten time faster than learning from scratch. Using the prior knowledge by itself appears as a good choice if only very few training samples are available but looses its advantage when the dimension of the training set increases. Passing from SA-SA and FA-FA to SA-FA we can also notice that the results for Prior Average show a small



Fig. 5. Hand posture and force signals dataset [14]. Classification rate obtained averaging over all the subjects as a function of the number of samples in the training set. The title of each figure specifies if the data used as source and target are registered in Still-Arm (SA) or Free-Arm (FA) setting.



Fig. 6. Hand posture and force signals dataset [14]. Correlation coefficient obtained averaging over all the subjects as a function of the number of samples in the training set. The title of each figure specifies if the data used as source and target are registered in Still-Arm (SA) or Free-Arm (FA) setting.



Fig. 7. Hand posture and force signals dataset [14]. Classification and Regression in the SA-SA setting for the best and worst subjects. With best and worst we mean the subjects for which the difference in performance between learning with adaption and learning from scratch is respectively maximum and minimum.



Fig. 8. Hand posture and force signals dataset [14]. Maps of the beta values for the three adaptive methods in classification, SA-SA, obtained for 210 training samples. The title of each figure indicates the adaptive method that produced the corresponding beta weights, in particular for Multi-perclass-Adapt we are showing the average values over the four classes (3 grasp postures plus rest). The rows 1 and 9 in all the matrices correspond respectively to the best and worst subject in classification considered in Figure 7, first and second plots from the left.



Fig. 9. Ninapro dataset [16]. Classification rate obtained averaging over all the subjects as a function of the number of samples in the training set. The title of each figure indicates the the number of subjects and hand postures considered.

drop (46.3%, 45.5%, 44.3%) related to the change in domain between the data used for pre-trained model and the one used for the new subject. The increasing difficulty of the task can be also evaluated by the progressive decrease in performance of Multi-perclass-Adapt at the very first step in the three cases: SA-SA 63.6%, FA-FA 62.7%, SA-FA 60.0%.

The corresponding regression results are reported in Figure 6. From the plot on the left we can notice that, in the SA-SA case, both the adaptive learning methods outperform No-Adapt (p < 0.03). However here Multi-Adapt and Best-Adapt performs almost equally (no statistical significant difference).

Figure 6 (center) shows that Best-Adapt is slightly worse than Multi-Adapt when passing to the FA-FA setting. Still the two methods are statistically equivalent and they show a significant gain with respect to No-Adapt only for more than 200 training samples (p < 0.03).

The problem becomes even harder in the SA-FA case (Figure 6 right), here Multi-Adapt outperforms No-Adapt only for more than 500 training samples (p < 0.03).

Globally the increasing difficulty of the three regression task passing from left to right in Figure 6 is demonstrated by the general drop in performance. Although we decided to show the correlation coefficient results, the corresponding MSE would lead to the same conclusions.

B. Ninapro [16]

For the Ninapro dataset, we shuffled randomly the training set and we considered 36 learning steps each with 30 samples reaching a maximum of 1080 training data.

Figure 9 (left) reports the obtained classification rate at each step when considering 10 subjects for the 6 grasp postures plus rest. The plot shows that all the adaptive methods performs almost as No-Adapt, in particular for less than 200 samples there is no statistical difference among learning from scratch, learning with adaption or using directly the prior knowledge (the fair comparison is with Prior Average and Prior Start). It is important to remark that the "few sample" range grows together with the number of considered classes: the samples are selected randomly and it is necessary a minimum amount of samples per class to get meaningful classification results. Only Multi-perclass-Adapt outperfoms No-Adapt (p < 0.05) with an average advantage of 2.5% in recognition rate for more than 200 samples.

Figure 9 (right) show the corresponding results in case of 20 subjects. On average No-Adapt and Prior Average perform almost equally to the previous case (with 10 subjects), showing that the average learning capability per subject is almost stable in a fixed range. On the other hand Prior Test and Prior Start present an increase in performance: the higher is the number of available prior models, the higher is the probability to find useful information for the new problem. Moreover, here Multiperclass-Adapt outperforms both Best-Adapt and No-Adapt (p < 0.001) with an average gain of 6% with respect to learning from scratch.

C. Discussion

As a general remark we can state that the three proposed adaptive methods (Multi-perclass-adapt, Multi-Adapt and Best-Adapt), improve the learning performance to different extents if prior-knowledge contains useful information for the new task, and never harm if any good match between the data of the new subject and the old source subjects is found. To further demonstrate this statement, Figure 7 shows the classification and regression results on SA-SA data respectively for the subject that have the maximum (best) and the minimum (worst) difference in recognition and regression performance with adaptation compared to No-Adapt. The worse-case subject represents the paradigmatic case of no previous models matching the current distribution; as a consequence the parameter β (β) is set automatically to a small value (to a vector of small norm). In this case there is essentially no transfer of prior knowledge. More insight on this point is given by Figure 8. Here we are mapping the beta values for each adaptive model in a specific learning step (210 training samples) of the classification SA-SA experiment. Best-Adapt chooses only one prior model as reference, while Multi-Adapt can rely on more than one known subject. For Multi-perclass-Adapt we show the average beta values over

the four classes (3 grasps plus rest). The results are consistent to each other: e.g. for subject 1 (1st row in the matrices), all the adaptive methods choose subject 8 as the most relevant, Multi-Adapt gives credit also to subject 2 and the same happens for Multi-perclass-Adapt which has more freedom in weighting each class and finds also subject 9 a bit useful. Actually subject 1 corresponds to the best subject, with the corresponding classification performance reported in Figure 7 (first from the left). Subject 9 is instead the worst one (Figure 7 second from the left), and the 9th row of all the matrices of Figure 8 actually indicates that all the beta values are small.

It is reasonable to claim that the overall performance of the adaptive methods would increase along with the number of stored models, since this would mean a larger probability of finding matching pre-trained models. This is confirmed by the results on the Ninapro dataset. In the long run, a large database of sEMG signals and force measure, with subjects possibly categorized (per age, sex, body characteristics, etc.) in order to avoid too hard a computational burden, would definitively help getting uniformly better performance.

Regarding the use of prior knowledge on a new problem, we point out here that, without an appropriate way to (a) choose the best prior knowledge model and (b) to weight and combine it with the new information, it is only partially helpful. In fact, Prior Test shows that possibly tuning on the test, it can be found one prior knowledge model that is useful for the new problem at the beginning but becomes neglegible in case of many available training samples. On the other hand, the Prior Average line corresponds to an attempt to use directly a flat combination of all the pre-trained models on a new subject: the obtained performance show that this is not a good solution.

Finally we briefly discuss the choice of the learning parameter C. Here we followed the standard approach in the community, and kept the the parameter C fixed using the best value obtained from cross validation on the known subjects. Still, one might argue that the best way to define it is to optimize it by using the available training samples of the target subject, separately for each learning approach. For the proposed adaptive methods, this would imply to define C together with β , leading to a non-convex problem with also a great increase in computational complexity.

VI. CONCLUSION

The results presented in this paper clearly show that machine-learning-based classification and regression applied to surface EMG can be improved by means of re-using previous knowledge. In particular, we start from SVM models previously built by training on a pool of human subjects, to boost the training time of a LS-SVM to new subjects. All the proposed adaptive methods show a significant gain in recognition rate for grasp type classification and in correlation coefficient for regression when predicting the applied force, with respect to learning from scratch on the new subject. Notice that the classification error/regression accuracy values shown here are in many cases below the best results obtained in competing literature (an almost comprehensive table appears in [3], page 725); but here the point is that of showing the comparison with non-adaptive baselines.

A comprehensive analysis of the practical applicability of our methods on real patients is out of scope here; hopefully however, our results show that the presented method can be used in any (sEMG classification/regression) scenario.

The overall idea is that a prosthesis could be embedded with additional, pre-existing knowledge before being shipped out to the generic patient. This needs to be done once and for all and, most likely, for a large pool of healthy subjects and/or amputees of diverse condition, age and type of operation, and degree of muscle remnant fitness. The fact that the freearm condition consistently benefits as well from the proposed technique — essentially to the same extent as the controlled one — is a very promising hint, meaning that one could potentially pre-train a prosthesis *in a laboratory* and then ship it outside, and still give a significant benefit of the patient with respect to the learning-from-scratch case.

The databases we used consists of intact subjects only, but it is believed that trans-radial amputees can generate similarly accurate signals ([19] is the most recent result on this topic), so this seems no disruptive objection to the applicability of the method. The project NinaPro (http://www.idiap.ch/project/ ninapro/) is currently concerned with collecting such a large database of mixed subjects. If confirmed on data acquired from amputees, the current result could pave the way to a significantly higher acceptance of myoprostheses in the clinical setting. As future work it would be also interesting to enlarge the presented approaches to more specific ongoing learning condition on the new subject, covering the hypothesis of an increasing number of hand postures.

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The database presented in [14] and used in this work has been collected and refined in 2009 at the Robotics, Brain and Cognitive Sciences Department of the Italian Institute of Technology, Genova, Italy, mainly by Angelo Emanuele Fiorilla. We would like to thank him and Giulio Sandini of the same Institute for making the database available to us.

APPENDIX

CLOSED FORMULA FOR THE LEAVE-ONE-OUT PREDICTION

We show here that, following the same steps presented in [39], it is possible to demonstrate the Proposition 1 obtaining the closed formula for the leave-one-out prediction in (12). We start from

$$\boldsymbol{M} \begin{bmatrix} \boldsymbol{a} \\ \boldsymbol{b} \end{bmatrix} = \begin{bmatrix} \boldsymbol{y} - \beta \hat{\boldsymbol{y}} \\ 0 \end{bmatrix} .$$
(28)

and we decompose M into block representation isolating the first row and column as follows:

$$\boldsymbol{M} = \begin{bmatrix} \mathbf{K} + \frac{1}{C}\mathbf{I} & \mathbf{1} \\ \mathbf{1}^T & \mathbf{0} \end{bmatrix} = \begin{bmatrix} m_{11} & \mathbf{m}_1^T \\ \mathbf{m}_1 & \mathbf{M}_{(-1)} \end{bmatrix} .$$
(29)

Let $a_{(-i)}$ and $b_{(-i)}$ represent the parameters of LS-SVM during the *i*-th iteration of the leave-one-out cross validation procedure. In the first iteration, where the first training sample is excluded we have

$$\begin{bmatrix} \boldsymbol{a}_{(-1)} \\ \boldsymbol{b}_{(-1)} \end{bmatrix} = \mathbf{P}_{(-1)} (\boldsymbol{y}_{(-1)} - \beta \hat{\boldsymbol{y}}_{(-1)}) , \qquad (30)$$

where $\mathbf{P}_{(-1)} = \mathbf{M}_{(-1)}^{-1}$, $\boldsymbol{y}_{(-1)} = [y_2, \dots, y_N, 0]^T$ and $\hat{\boldsymbol{y}}_{(-1)} = [\mathbf{w}' \cdot \phi(\boldsymbol{x}_2), \dots, \mathbf{w}' \cdot \phi(\boldsymbol{x}_N), 0]^T$. The leave-one-out prediction for the first training sample is then given by

$$\tilde{y}_1 = \mathbf{m}_1^T \begin{bmatrix} \mathbf{a}_{(-1)} \\ b_{(-1)} \end{bmatrix} + \beta \mathbf{w}' \cdot \phi(\mathbf{x}_1)$$
(31)

$$= \mathbf{m}_{1}^{T} \mathbf{P}_{(-1)} (\boldsymbol{y}_{(-1)} - \beta \hat{\boldsymbol{y}}_{(-1)}) + \beta \mathbf{w}' \cdot \phi(\boldsymbol{x}_{1}) . \quad (32)$$

Considering the last N equations in the system in (28), it is clear that $[\mathbf{m}_1 \ \mathbf{M}_{(-1)}][\boldsymbol{a}^T, b]^T = (\boldsymbol{y}_{(-1)} - \beta \hat{\boldsymbol{y}}_{(-1)})$, and so

$$\tilde{y}_{1} = \mathbf{m}_{1}^{T} \mathbf{P}_{(-1)}[\mathbf{m}_{1} \mathbf{M}_{(-1)}][a_{1}, \dots, a_{N}, b]^{T} + \beta \mathbf{w}' \cdot \phi(\boldsymbol{x}_{1})$$

$$= \mathbf{m}_{1}^{T} \mathbf{P}_{(-1)} \mathbf{m}_{1} a_{1} + \mathbf{m}_{1}^{T} [a_{2}, \dots, a_{N}, b]^{T} + \beta \mathbf{w}' \cdot \phi(\boldsymbol{x}_{1}) .$$
(33)

Noting from the first equation in the system in (28) that $y_1 - \beta \mathbf{w}' \cdot \phi(\mathbf{x}_1) = m_{11}a_1 + \mathbf{m}_1^T [a_2, \dots, a_N, b]^T$, we have

$$\tilde{y}_1 = y_1 - a_1 (m_{11} - \mathbf{m}_1^T \mathbf{P}_{(-1)} \mathbf{m}_1)$$
 (34)

Finally, using $\mathbf{P} = \mathbf{M}^{-1}$ and applying the block matrix inversion lemma we get,

$$\mathbf{P} = \begin{bmatrix} \mu^{-1} & -\mu^{-1}\mathbf{m}_{1}\mathbf{P}_{(-1)} \\ \mathbf{P}_{(-1)} + \mu^{-1}\mathbf{P}_{(-1)}\mathbf{m}_{1}^{T}\mathbf{m}_{1}\mathbf{P}_{(-1)} & -\mu^{-1}\mathbf{P}_{(-1)}\mathbf{m}_{1}^{T} \end{bmatrix}$$

where $\mu = m_{11} - \mathbf{m}_1^T \mathbf{P}_{(-1)} \mathbf{m}_1$ and noting that the system of linear equations (28) is insensitive to permutations of the ordering of the equations and of the unknowns, we have

$$\tilde{y}_i = y_i - \frac{a_i}{P_{ii}} \ . \tag{35}$$

Let $\boldsymbol{a} = \boldsymbol{a}' + \beta \boldsymbol{a}'', [\boldsymbol{a}'^T, b']^T = \boldsymbol{P}[\boldsymbol{y}^T, 0]^T$ and $[\boldsymbol{a}''^T, b'']^T = \boldsymbol{P}[\hat{\boldsymbol{y}}^T, 0]^T$, from the equation above we get :

$$\tilde{y}_i = y_i - \frac{a'_i}{P_{ii}} + \beta \frac{a''_i}{P_{ii}} .$$
(36)

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